

On some research and innovation challenges in AI

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www.irt-systemx.fr/en



Challenges and industrial applications in

- **Hybrid AI:** How to exploit industry knowledge of physical (scientific) and symbolic (semantic) nature in data-driven learning models.
- **Trustworthy AI:** Towards integrating AI into critical system engineering
- **Generative AI for industry:** How to evaluate and advance specialized generative AI models for industrial applications

Challenges and industrial applications in

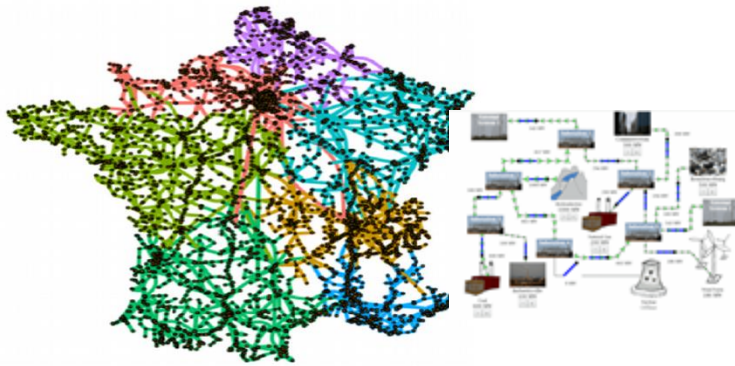
- **Hybrid AI:** How to exploit industry knowledge of physical (scientific) and symbolic (semantic) nature in data-driven learning models.
- Trustworthy AI: Towards integrating AI into critical system engineering
- Generative AI for industry: How to evaluate and advance specialized generative AI models for industrial applications

Motivation: Some physical problems in Industry

Related to the design and supervision of complex (physical) systems

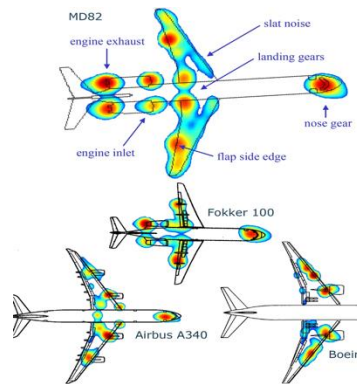
- Covering various fields in physics (mechanics, fluid dynamics, aerodynamics, electromagnetism ...)
- In a wide variety of Applications in industry, in particular in numerical **simulation**

Electricity (power grids)



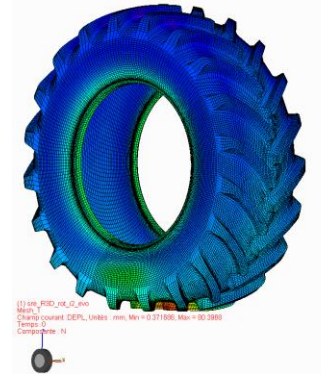
Picture from **Marot, A., et al.** (2018).

Aerodynamics



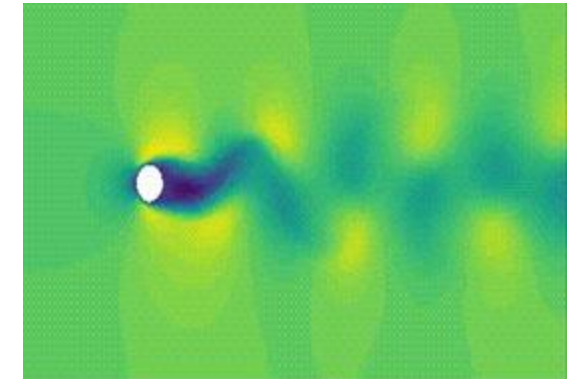
Picture form Merino-Martínez *et al.* *CEAS Aeronautical Journal* (2019).

Solid Mechanics pneumatics



From HSA – SystemX

Fluid Flows/Dynamics



from Emmanuel Menier (PhD, LSIN/SystemX, 2024)

Domain Challenges : Physical systems that are

(eg. , in Computational Fluid Dynamics – CFD, Turbulence, Flows)

- Complex to model/solve analytically
- Computationally expensive to solve numerically

- Physics knowledge to guide learning

Integrating geometric priors in learned representations (Bronstein 2017)

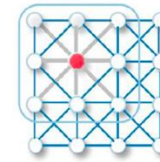
Geometric deep learning, **GNN** and neural passing message (Arjona Martínez 2019)

- **Differential equations** to improve deep learning

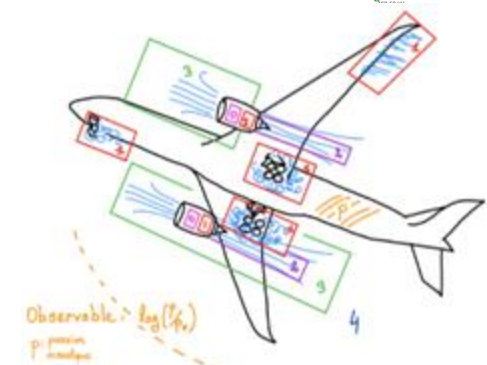
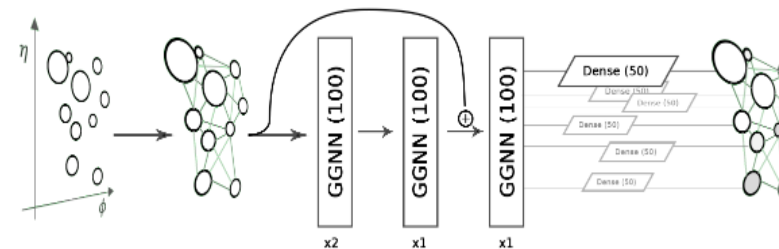
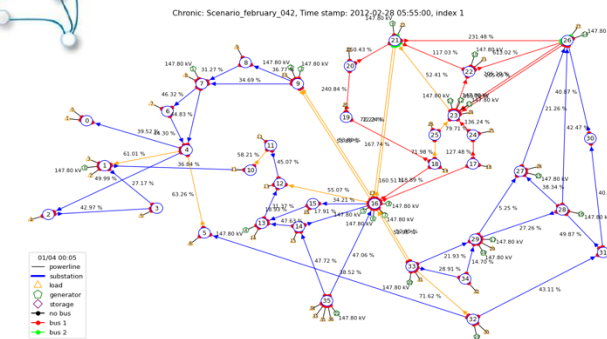
Neural differential equations, diffusion models, ...

- **Deep learning** to solve differential equations

Hypersolvers, hybrid solvers, neural operators, PINNs - Physics-Informed NNetworks, ... (Raissi 2019)



Power Grid (HSA Project)
Substations and lines



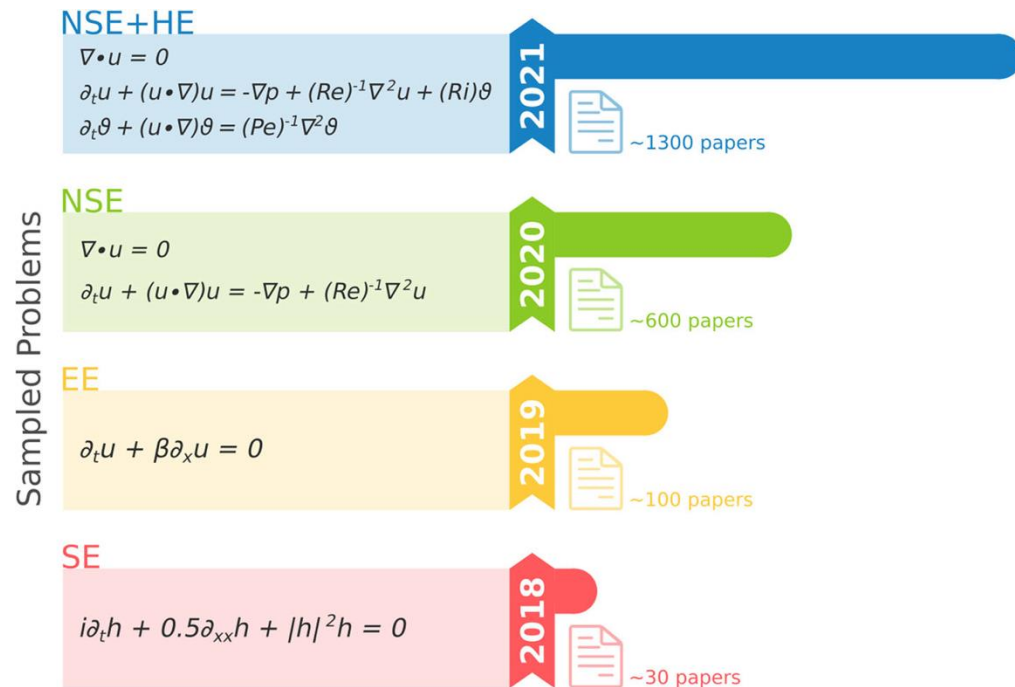
⇒ **Promising for engineering**, it allows :

- the integration of analytic knowledge from physical laws governing the engineering systems, to augment statistical knowledge learned from data (eg. by deep learning)
- reducing the high cost of physical simulation, in particular in industry

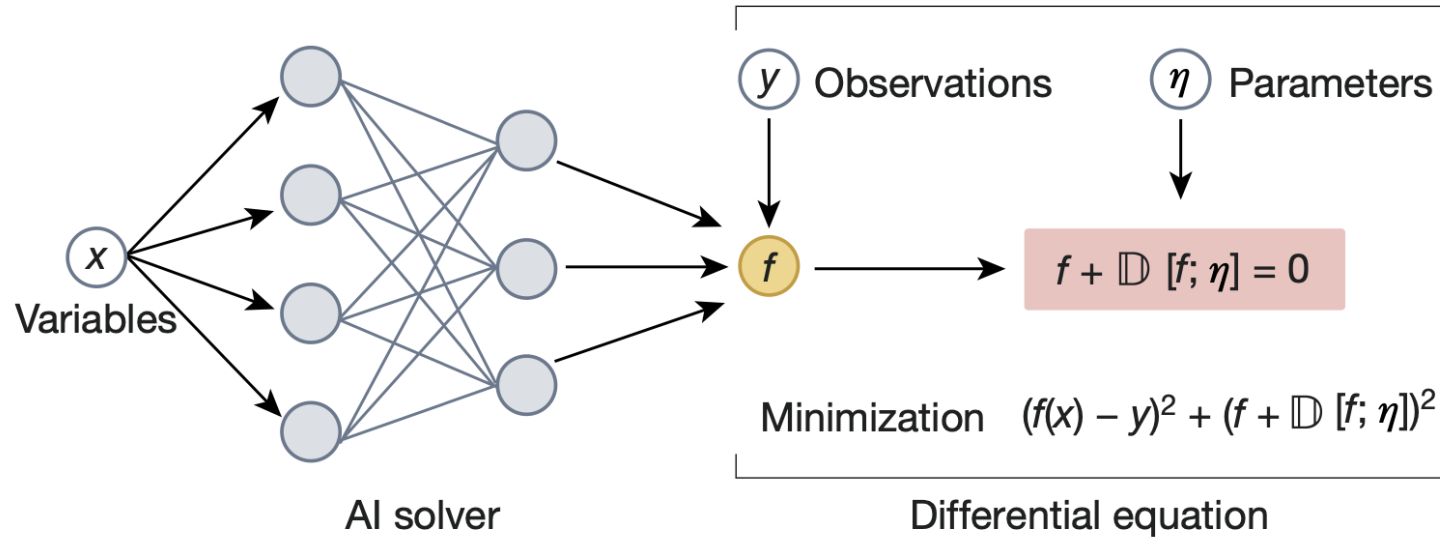
Scientific Challenges

- Problems highly-nonlinear, high-dimensional, with complex structures (eg. organized in graphs...)
- Need for adapted NN architectures: GNNs, Deep AEs ..

- ➔ Enables prior scientific knowledge based on physics to be taken into account in data-driven machine learning methods e.g including PINNs - Physics-Informed Neural Nets (Raissi's paper in 2019)
- ➔ Has been *successfully and increasingly* applied to solve a wide variety of linear and nonlinear problems in physics, covering various fields like mechanics, fluid dynamics, thermodynamics, electromagnetism ... including :



- Solving Navier–Stokes equations coupled with the corresponding temperature equation for analyzing heat flow convection (NSE+HE). Cai et al, 2021
- Solving incompressible Navier–Stokes equations (NSE). Jin et al., 2020.
- Solving Euler equations (EE) that model high-speed aerodynamic flows. Mao et al, 2019
- Solving the nonlinear Schrödinger Equation (SE).



A neural framework for solving PDEs, where

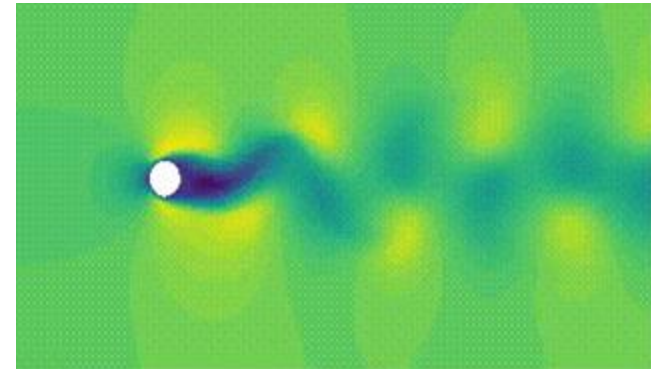
- the AI solver is a PINN trained to estimate target function f .
- The derivative of x is calculated by automatically differentiating the NN's outputs.
- When the differential equation parametrized by (η) is unknown, it can be estimated by solving a loss that optimizes both the functional form of the equation and its fit to observ y .

- Eg. Learning Computational Fluid Dynamics

- Navier-Stokes Equations: fundamental partial differential equations (**PDE**) that describe the flow of incompressible fluids.

C.L. M. H. Navier, Memoire sur les Loix du Mouvements des Fluides, Mem. de l'Acad. d. Sci., 6, 398 (1822)
C.G. Stokes, On the Theories of the Internal Friction of Fluids in Motion, Trans. Cambridge Phys. Soc., 8, (1845)

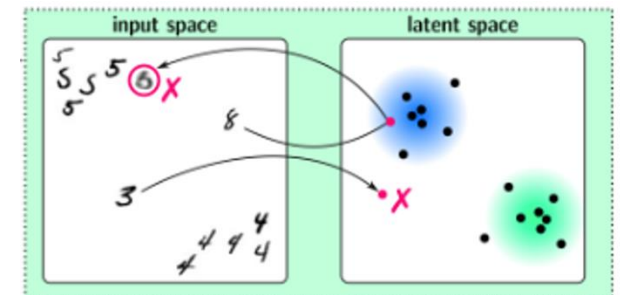
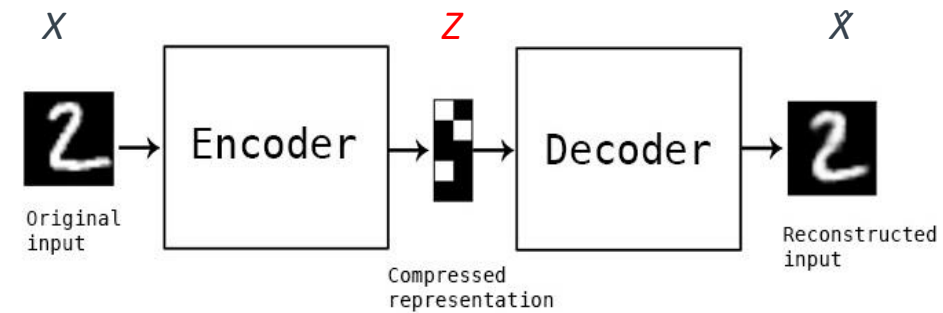
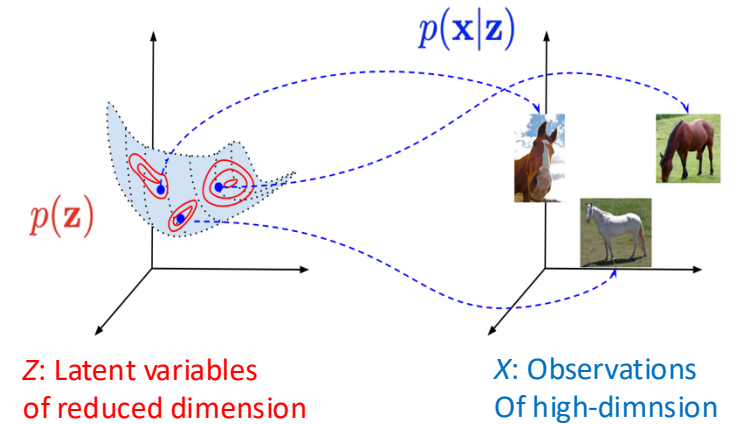
- Challenge: **High-Dimensional non-linear** Physical Equations



Credit: Emmanuel Menier, PhD LISN/SystemX

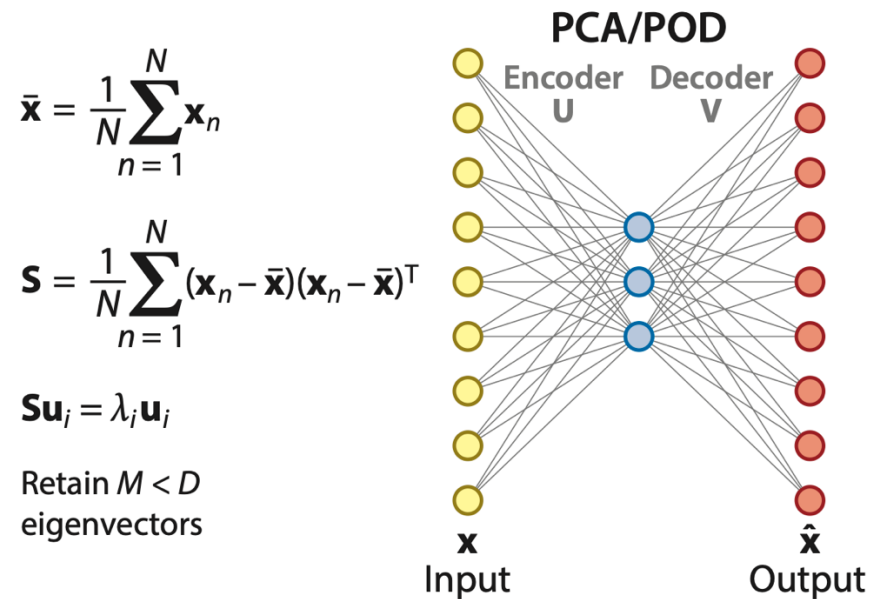
Latent Variable Models: A family of probabilistic models capable of inferring the intrinsic latent structure (of reduced dimension) of the data

- **Auto-Encoders - AE** (LeCun 1987): The **encoder** projects the input \mathbf{X} (of high-dimension dimension) in a compressed latent representation \mathbf{Z} (the **code**) to reconstruct it using the **decoder** with output $\hat{\mathbf{X}}$
- ➔ Learning by minimizing the reconstruction error between $\hat{\mathbf{X}}$ and \mathbf{X} . The smaller the error, the better the compressed representation \mathbf{Z} .
- **Variational Auto-encoders - VAE** (Kingma & Welling 2014) improve the representational capabilities of AEs by regularizing the latent space with a Gaussian prior, coupled with a **variational learning**
- => can learn complex distributions.
- **Deep NNets** are excellent candidates

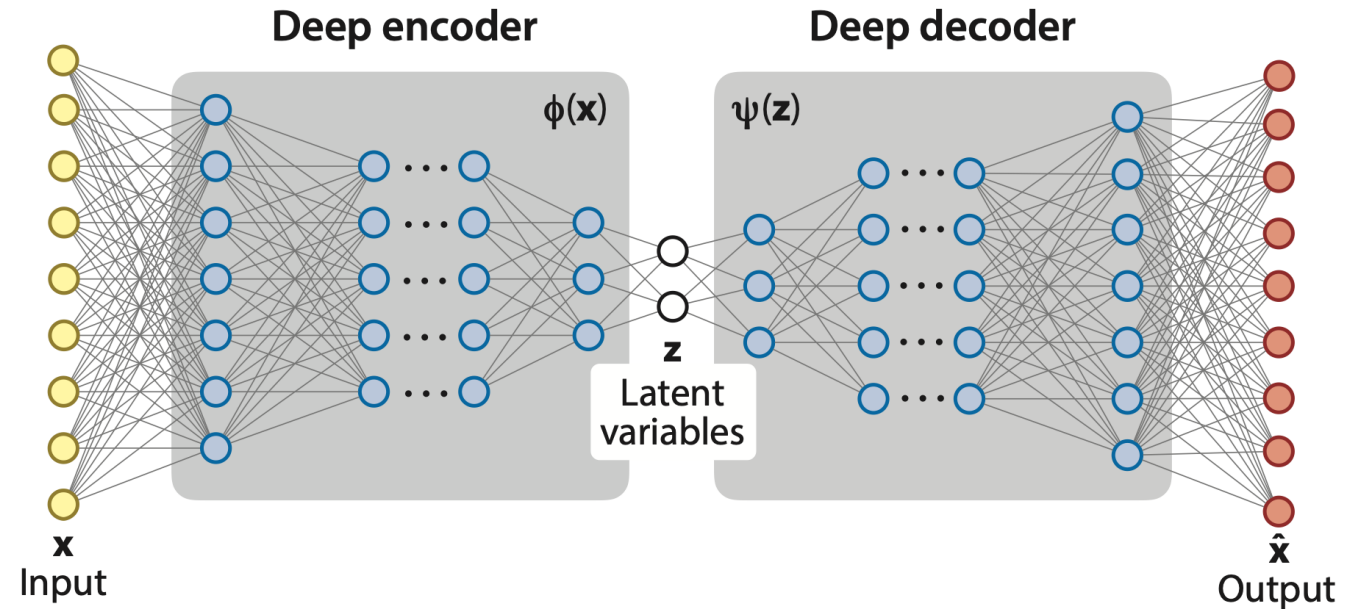


- Nnets are capable to recover highly non-linear relationships in the data
- Adapted architectures that work in a low-dimensional (latent) space

Shallow / Linear



Deep / Non-Linear



Auto-Encoding Deep Nets

POD: proper orthogonal decomposition
 PCA: principal component analysis



Intelligence
artificielle
et ingénierie
augmentée

Artificial Intelligence
and Augmented Engineering

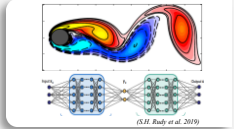
- a program with **6 R&D collaborative projects** on concrete **industrial use cases**
- Area: Hybrid AI
- 20+ industrial and academic partners
- ~12M€

Advance project
Thesis / Postdocs / Shared work

HSA: Simulation/machine learning hybrid modeling

How industrial solvers and learning models can enrich each other ?

01



AFS: Agility and fidelity of simulations

How to improve agility and fidelity of simulation in complex systems design?

02



S2I: Industrial infrastructure supervision

How to improve decision-making on distributed industrial systems via machine learning techniques ?

03



SAA: Augmented multi-agent simulation

How can multi-agent models benefit from real data and bring out atypical situations?

04



SMD: Business Semantics for Multi-source Data Mining

How to link heterogeneous data with established practical knowledge?

05



CAB: Cockpit and Bidirectional Assistant

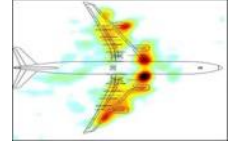
How to develop a virtual assistant that learns from expert and learns to the expert

06



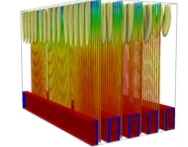
AIRBUS

AIRBUS: Aircraft aero-acoustic performance



Air Liquide

Air Liquide: Steam methane reforming



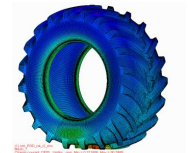
EDF

EDF: Energy modeling of buildings



MICHELIN
LES PNEUS SONT FAITS EN FRANCE

Michelin: 3D rolling tire



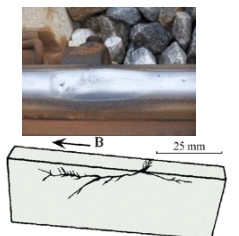
Rte

RTE : Augmented simulator for electrical grid management



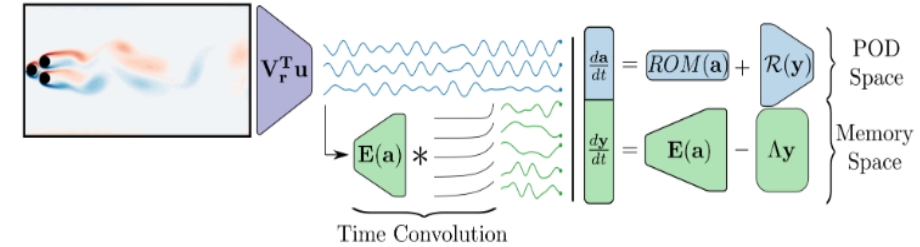
SNCF

SNCF: Forecasting crack propagation in rails

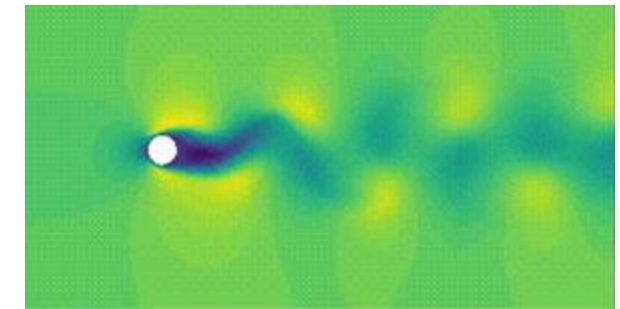
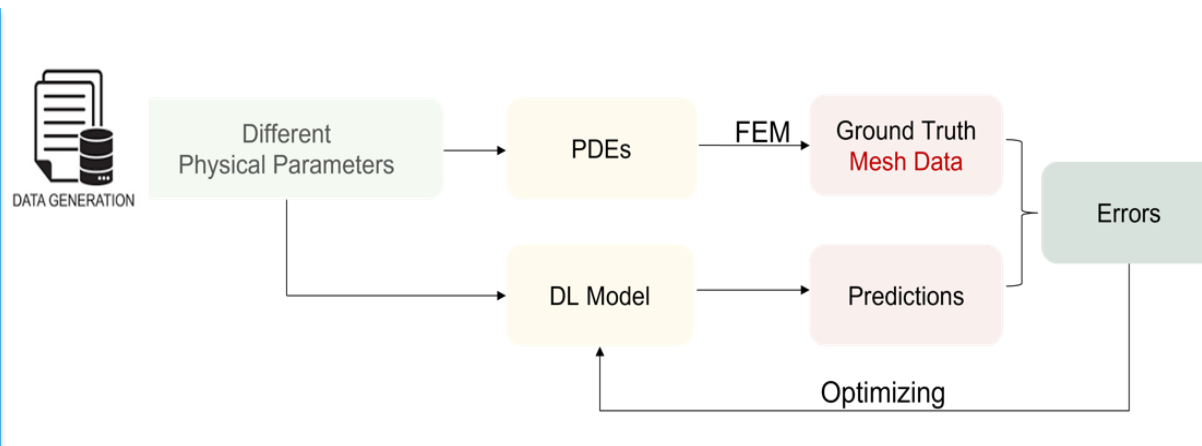


Challenges and possible solutions (studied as part of the HSA project):

- Augmenting physical solvers with data-driven models that integrate physics constraints
- Building model architecture adapted to the complex physical structures/systems
- Reducing the simulation cost
- ➔ Surrogate models for physical simulation, aiming to Replace physical solvers with
- ➔ Deep learning intergrating physical constraints (eg. Deep Graph Nets for PDEs)
- ➔ Deal with high-dimensional, non-linear, and complex structur (e.g reduced modeling, ..)



High-Dimensional non-linear Physical Equations



Reduced models and deep learning for PDEs
PhD Thesis of E. Menier, 2024 (LISN, Inria/SystemX)

E. Menier et al., 2023. CD-ROM: Complementary Deep-Reduced Order Model. *Computer Methods in Applied Mechanics and Engineering* 410. [Read Online](#)

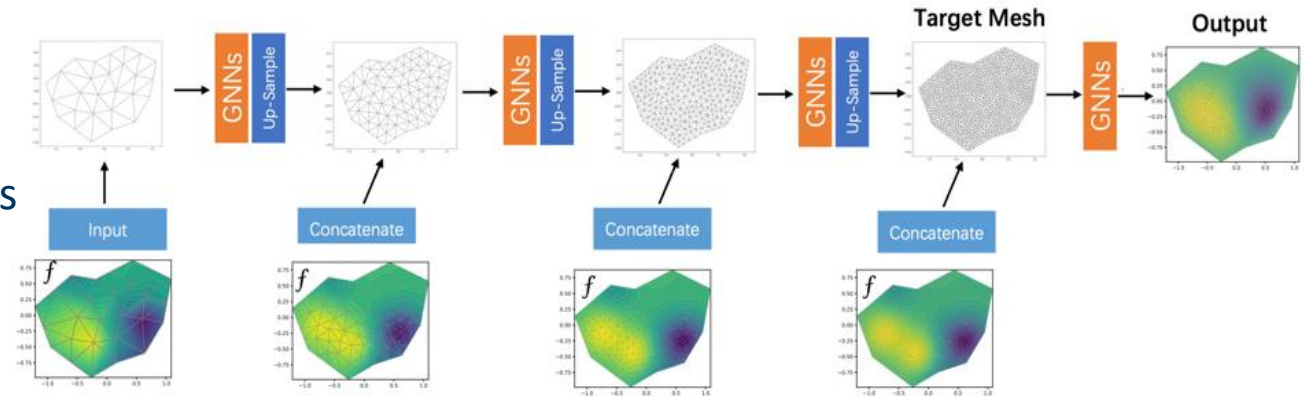
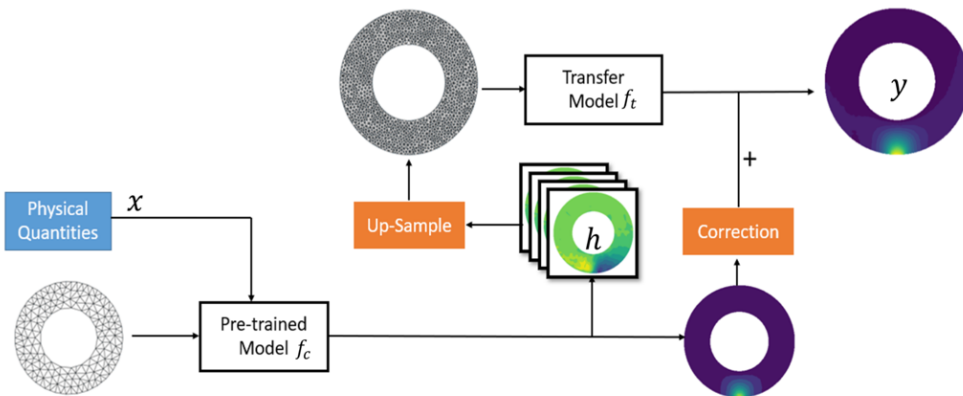
Deep Graph Neural Networks for Numerical Simulation of PDEs. PhD of W. Liu. 2023 (LISN, Inria/SystemX). [Read Online](#)

Graph Neural Nets for 3D meshes

More suitable, as they operate by construction on graphs

- Generic nature of the learned models
- Transfer learning for improved results
- Prediction can be improved via transfer learning:

from low fidelity (coarse mesh) to high fidelity (finer mesh) models



Wheel contact profile

Physics: contact equations

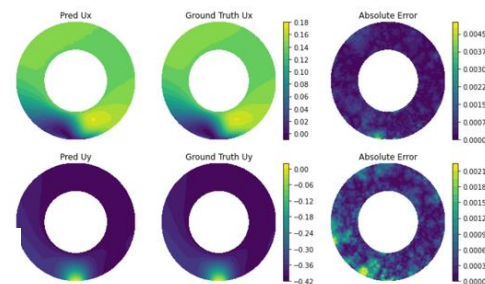
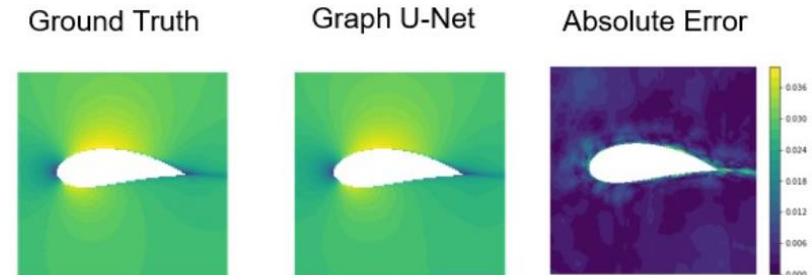
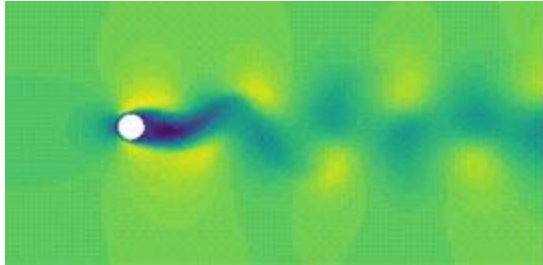


Figure 6.3: An example of wheel contact prediction

Modeling of the airflow profile around an aircraft wing (Air Foil)

Physics: Navier-Stokes equations





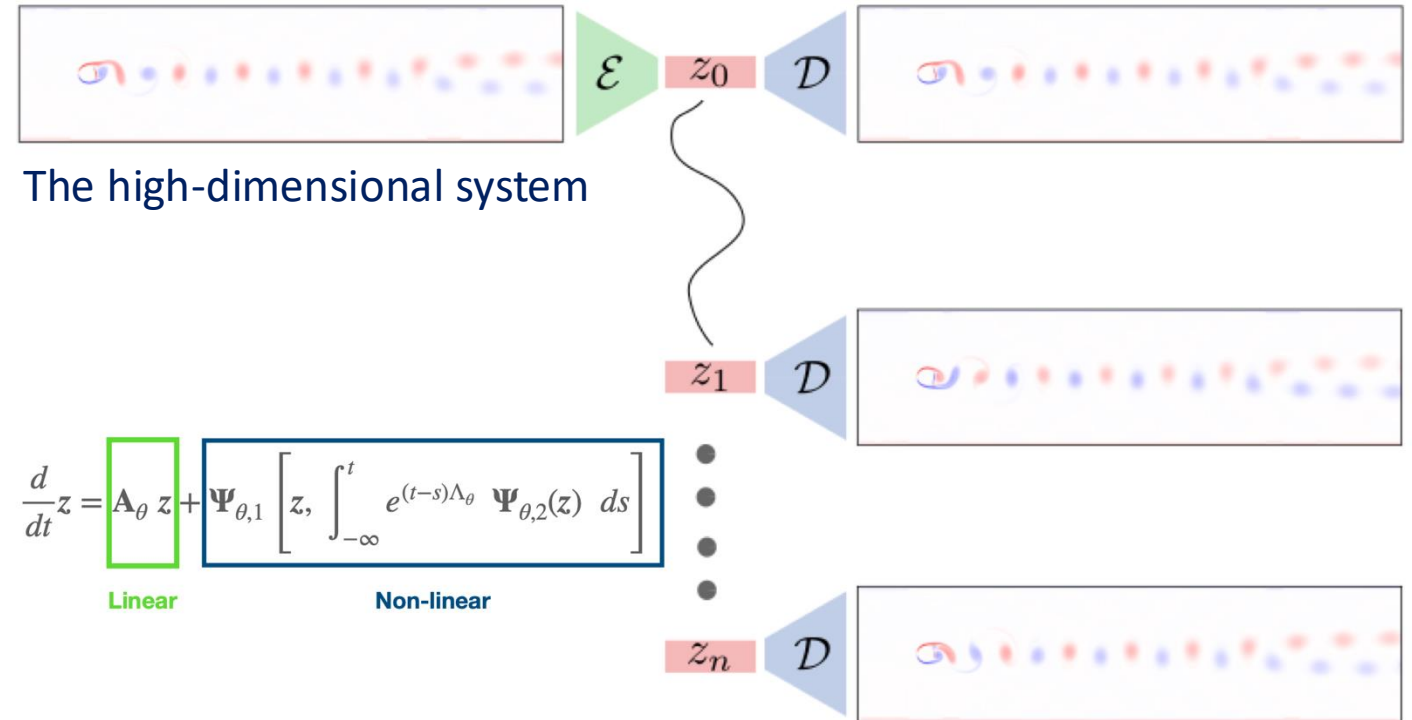
High-Dimensional non-linear Dynamical Systems:

Goals:

Recover the dynamics, non-linearity in a high-dimensional setting

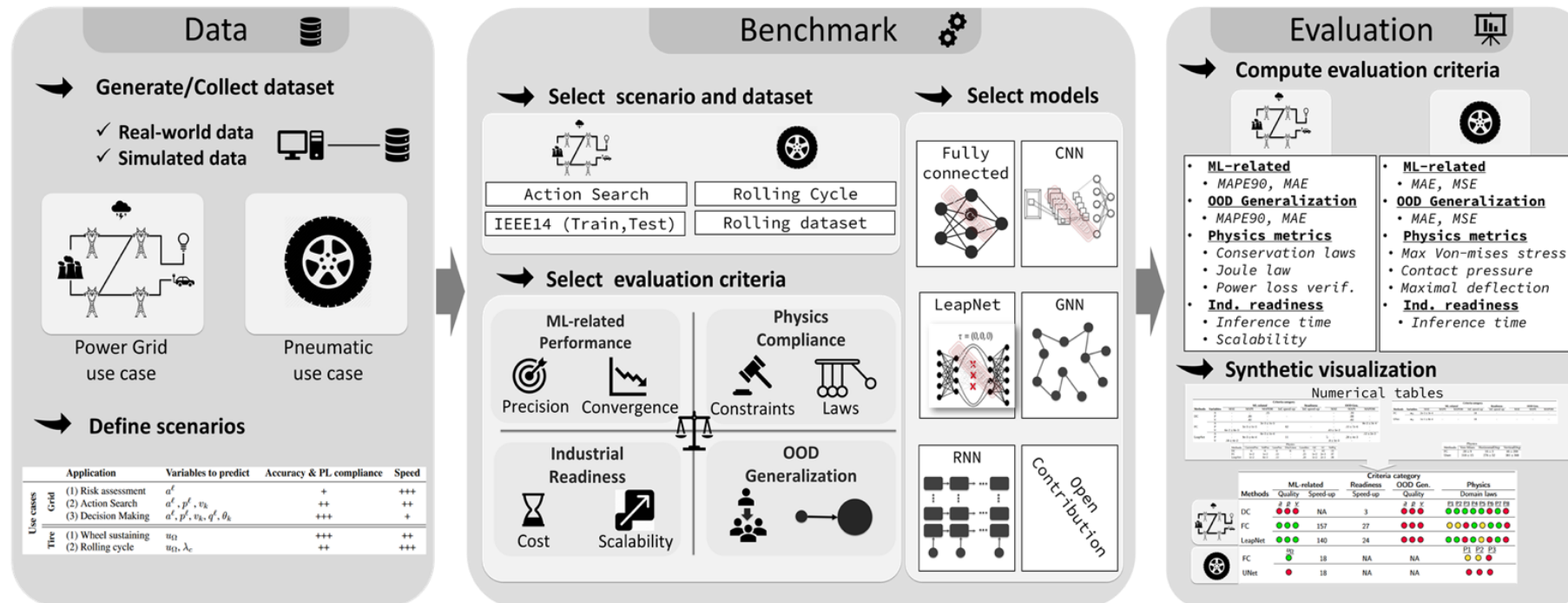
An Auto-Endore based architecture

Interpretable learning of effective dynamics (ILED) architecture:



The lower-dimensional representation (\mathbf{z}) is propagated in time using a linear and a non-linear part based on the Mori-Zwanzig formalism

- **How to validate hybrid (with physics) ML approaches ?**
 - Several evaluation criteria are required (statistical performance, physical compliance, generalization, etc)
 - Comparison of # ML methods on several specific physical problems => need for a common evaluation framework
- **Proposed solution for industry : LIPS “Learning Industrial Physical Simulation” benchmark suite** (*Result of the project HSA-IA2*)
 - 1st framework for the evaluation of physical simulators augmented by machine learning
 - 7 use cases integrated
 - Open-source Framework <https://github.com/IRT-SystemX/LIPS> Published at NeurIPS2022



LIPS hosts/ed the three following competitions:

<https://www.codabench.org/competitions/1534/>

<https://www.codabench.org/competitions/2378/>

<https://www.codabench.org/competitions/3282/>

MACHINE LEARNING FOR PHYSICAL SIMULATION CHALLENGE

128 PARTICIPANTS
1165 SUBMISSIONS

€7000 to be shared by the 5 winners (see prizes page)

ORGANIZED BY: Systemx
CURRENT PHASE ENDS: Never
CURRENT SERVER TIME: 8 Mai 2024 à 08:00 UTC+2
Docker image: lipsbenchmark/ml4physim:1.4

Get Started Phases My Submissions Results Forum

About

New ML4Physim challenge : The powergrid usecase

Competition Overview

This competition aims at promoting the use of ML based surrogate models to solve physical problems, through a task addressing a recently published dataset called **AirFRANS** related to **airfoil design (CFD simulation)**.

The competition will address the challenge of improving baseline solutions of the Airfoils design use case by building ML-based surrogate models. The overall aim is to improve the tradeoff between the precision of obtained solutions and the related computational cost.

Baseline	ML-related (40%)		Criteria category				Score (100%)
	Accuracy	Speed-up	Application-based content (30%)		Physics (20%)		
			OOO Accuracy	Speed-up	Domain laws		
GraphSAGE	1000	1000	1000	1000	1000	55.87	
FC	1300	1300	1300	1300	1300	44.57	
OpenFOAM	1	1	1	1	1	82.5	

MACHINE LEARNING FOR PHYSICAL SIMULATION CHALLENGE - POWERGRID USE CASE

31 PARTICIPANTS
0 SUBMISSIONS

ORGANIZED BY: Systemx
CURRENT PHASE ENDS: 14 Mai 2024 à 02:00 UTC+2
CURRENT SERVER TIME: 8 Mai 2024 à 08:04 UTC+2
Docker image: codalab/codalab-legacy:py37

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About

Prizes

General prizes:

- 1st Prize : 3000 €
- 2nd Prize : 2000 €
- 3rd Prize : 1000 €

Special prizes:

- Most accurate ML model (without speedup consideration) : 1000 €
- Best student solution : 1000 €

The general and special prizes are not cumulative. Winning one of the general prizes hinder the access to special prizes.

NEURIPS 2024 - ML4CFD COMPETITION

227 PARTICIPANTS
401 SUBMISSIONS

ORGANIZED BY: Systemx
CURRENT PHASE ENDS: 26 Octobre 2024 à 02:00 UTC+2
CURRENT SERVER TIME: 15 Octobre 2024 à 11:59 UTC+2
Docker image: lipsbenchmark/ml4physim:1.9

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about

The starting Kit is now available at : <https://github.com/IRT-SystemX/NeurIPS2024-ML4CFD-competition-Starting-Kit>

Competition Overview

The integration of machine learning (ML) techniques for addressing intricate physics problems is increasingly recognized as a promising avenue for expediting simulations. However, assessing ML-derived physical models poses a significant challenge for their adoption within industrial contexts. This competition is designed to promote the development of innovative ML approaches for tackling physical challenges, leveraging our recently introduced unified evaluation framework known as Learning Industrial Physical Simulations (LIPS). Building upon the preliminary edition held from November 2023 to March 2024, this iteration centers on a task fundamental to a well-established physical application: airfoil design simulation, utilizing our proposed AirFRANS dataset.

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→ The challenge: **Producing explanations**

There are several ways of producing explanations:

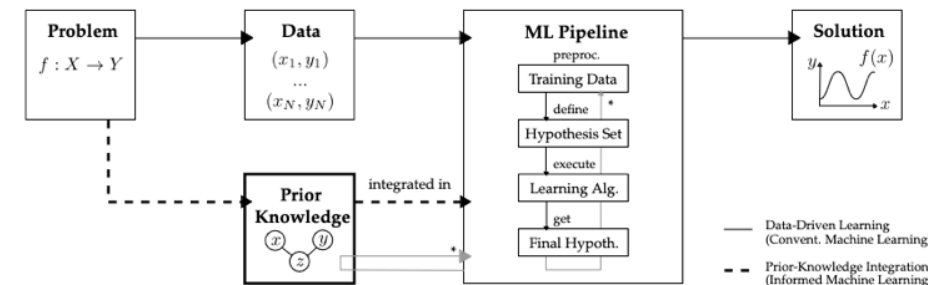
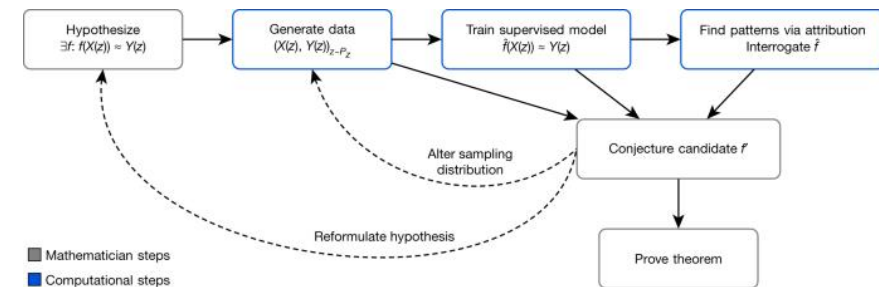
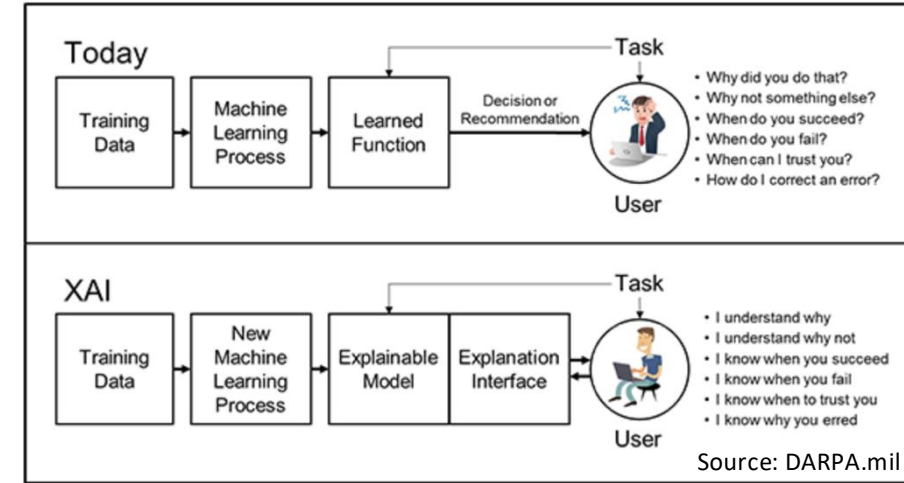
1. training the NNet to produce arguments at the same time as prediction
2. => or using a **hybrid approach** combining symbolic and neural methods

- Combining learning and knowledge graphs enables **business expertise to be integrated** and results to be **explained**.

→ Neuro-symbolic methods aim at bridging techniques from symbolic AI and deep learning:

- integrating a symbolic paradigm into a neural network
- E.g The ML model uses explicit symbolic knowledge, in the form of logic rules/ontologies, to specify desired properties for the NNet.

- Formal rules for explainability (Audemard, 2023)
- Improving Neural-Based Classification with Logical Background Knowledge (Ott 2023) (Battaglia 2018)



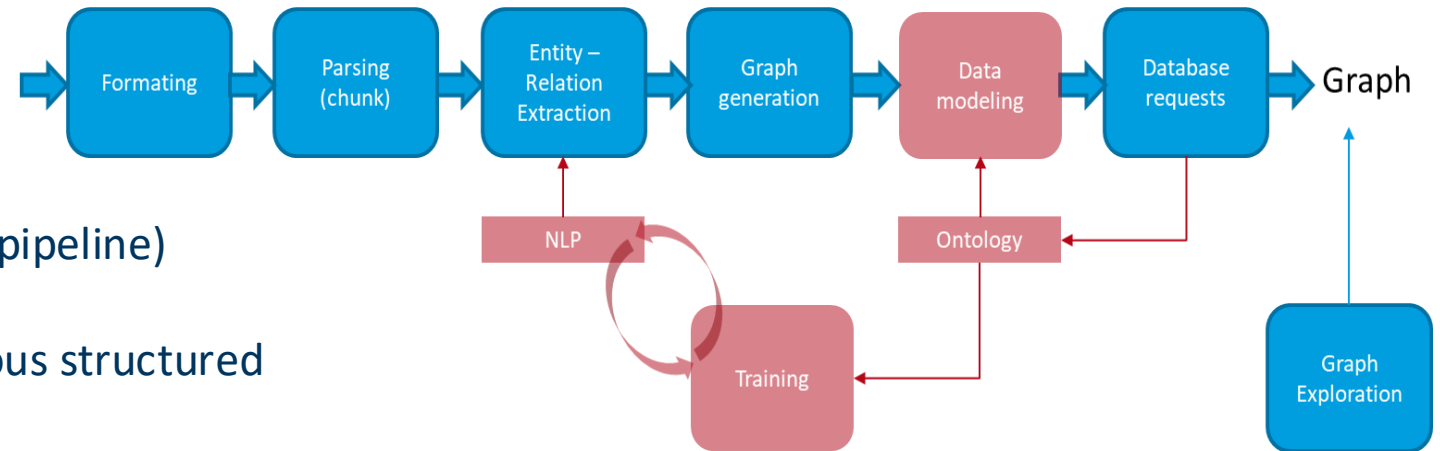
Framework:

Building ML-based on knowledge graphs from expert/business language data

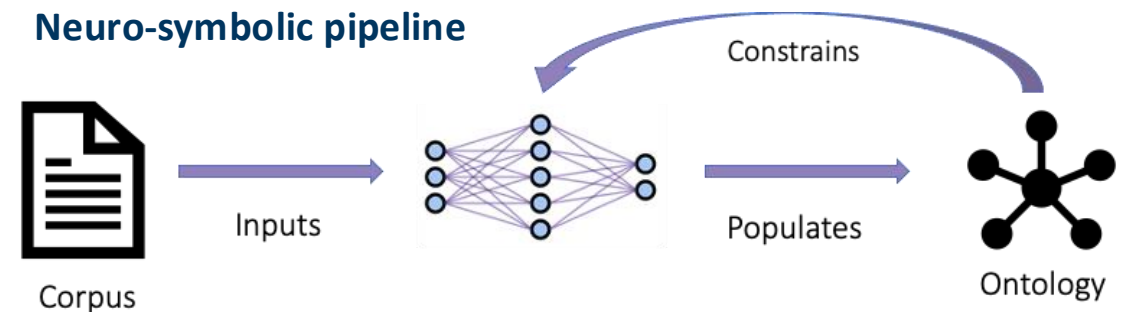
Approach (The Neuro-symbolic engineering pipeline)

- Information extraction from heterogeneous structured and semi-structured text corpora...
- NLP approach; Semantic annotation
- Taking into account domain rules/constraints in the numerical-AI based decision

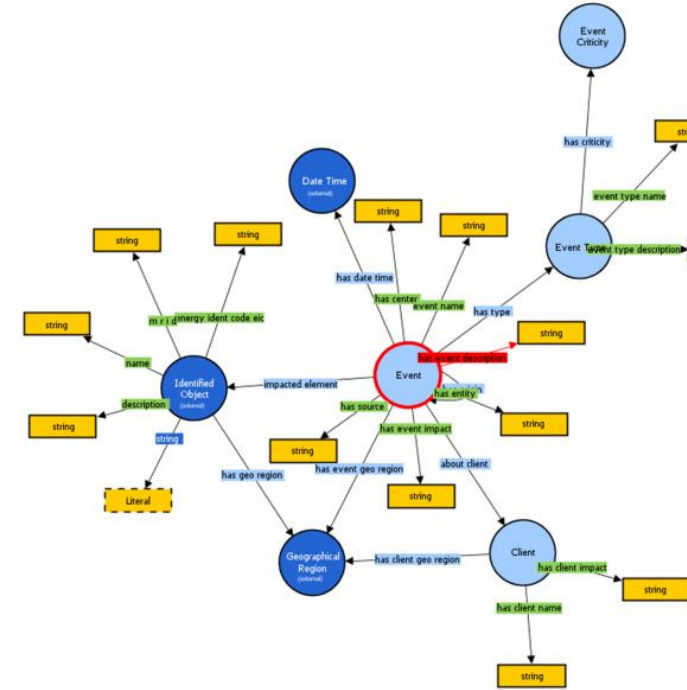
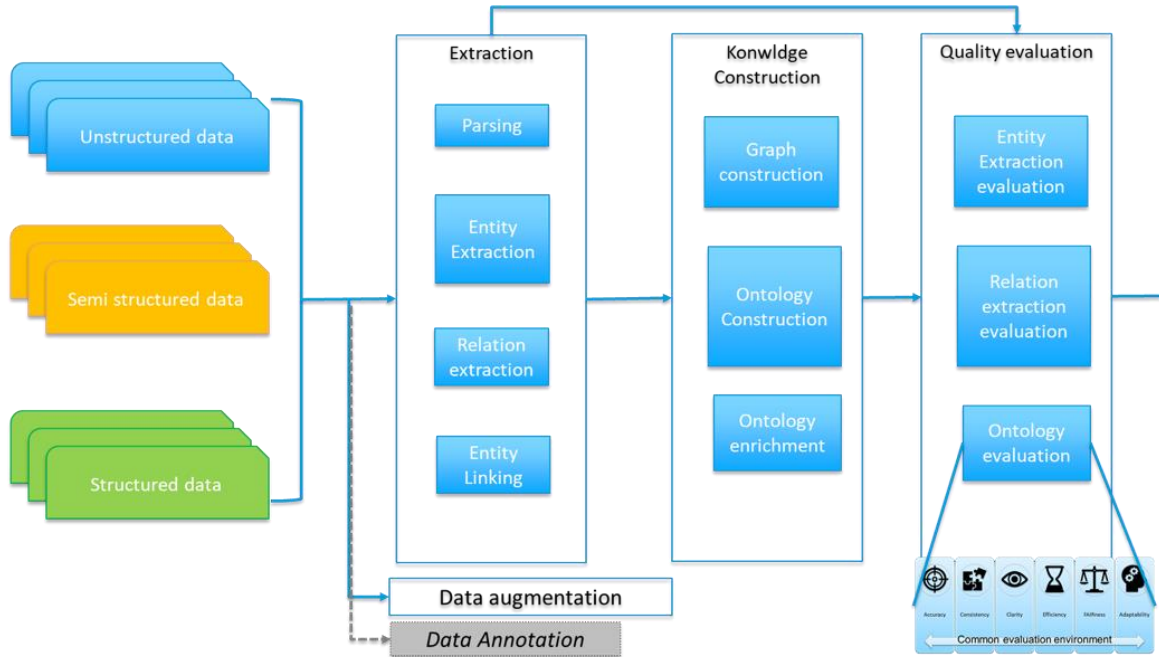
The Neuro-symbolic engineering pipeline: <https://www.irt-systemx.fr/projets/SMD/>



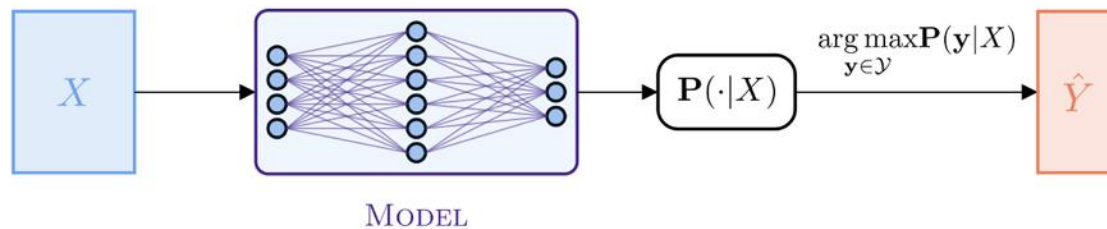
Neuro-symbolic pipeline



Ontology-based explanations :



Logic rules, to specify desired properties for the Nnet:



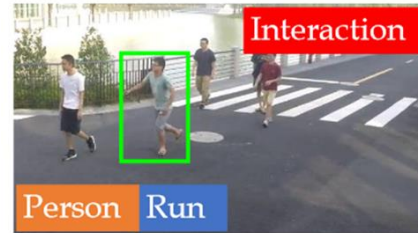
- => Insertion of logical rules at the inference step :
- Recalculate $P(y|X, \alpha)$ in lieu of the learnt $P(y|X)$
 - α is a rule encoding the validity of the prediction \hat{y}

Use case : Detection and characterization of atypical scenes in surveillance videos for crisis management

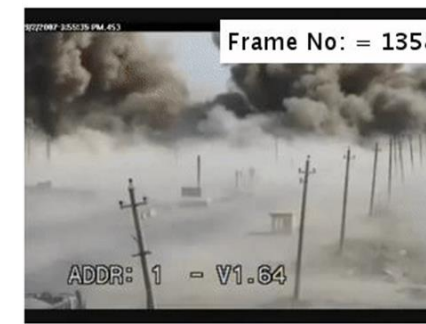


- identifying anomalies in video streams
- scene analysis and construction of contextualized graphs

**these shown examples are obtained on Public (not industrial) data*



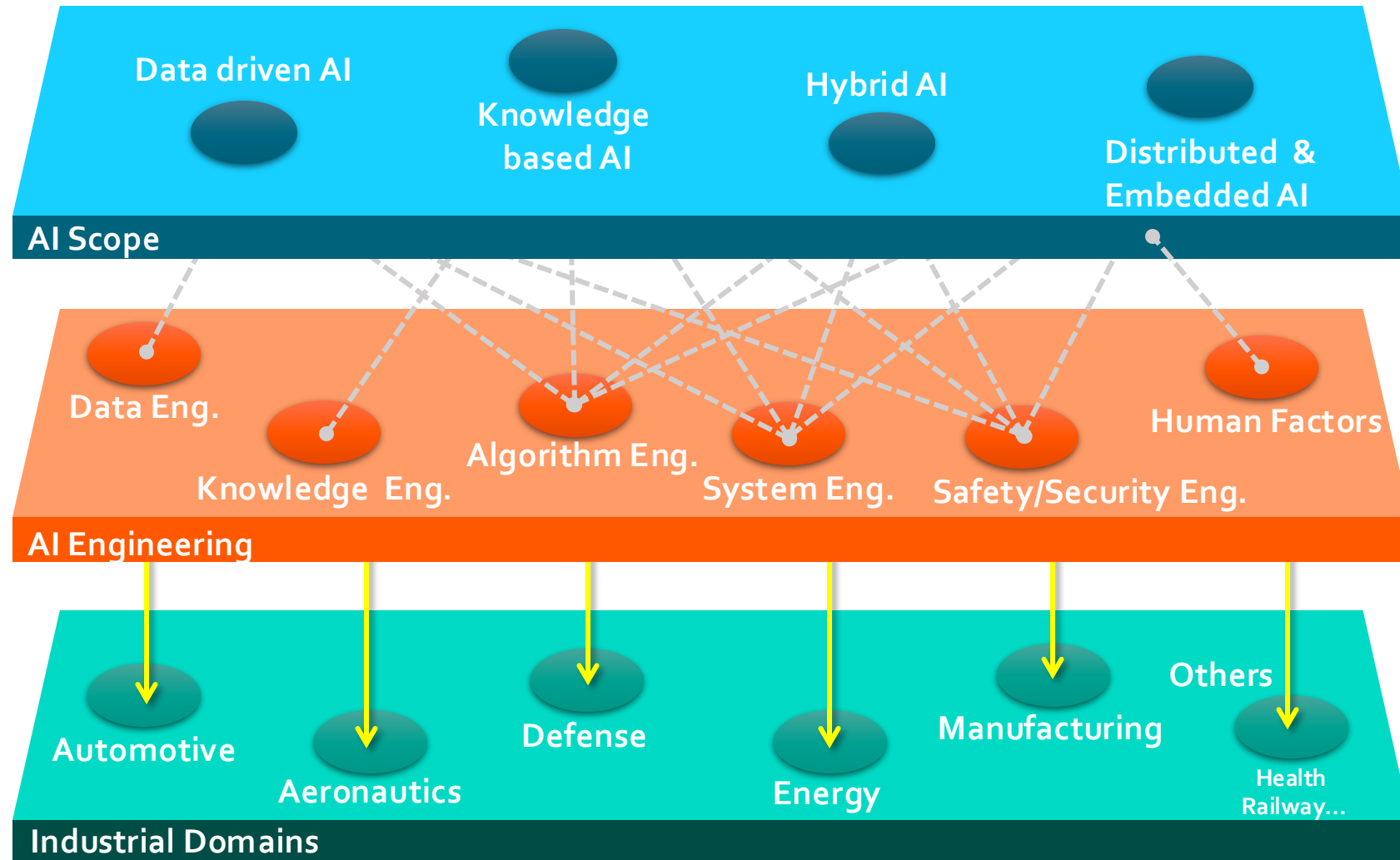
ShanghaiTech data (437 videos on 13 different locations, containing 130 abnormal events)



UCF-crime data (128 hours videos contain realistic anomalies including Abuse, Arrest, Arson, Assault, etc.)

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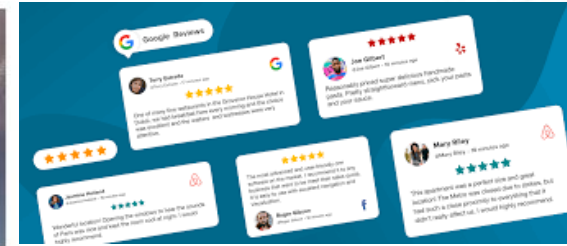




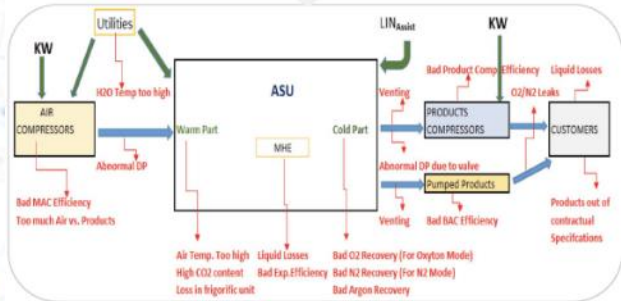
THALES
Building a future we can all trust



RENAULT

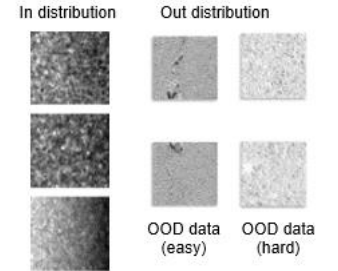


Valeo

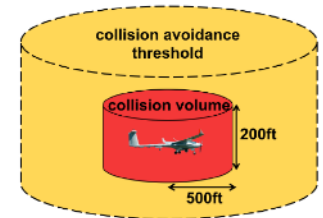


Air Liquide

Theme	Primary	Secondary
2D Vision	Scene understanding (Valeo) In autonomous driving	Aerial pictures (Thales LAS)
Visual inspection	Welding inspection (Renault)	Industrial control (Safran)
Time series prediction	Demand forecasting (Air Liquide) Eg. oxygen	
Time series anomaly detection	Plant efficiency monitoring (Air Liquide)	Virtual sensor (Airbus Helicopter)
Tabular data	ACAS XU (Airbus)	
NLP	Opinion mining (Renault)	
Hybrid ML Symbolic	Time dependent planning (Safran)	
Visual similarity	Re-identification (ATOS)	



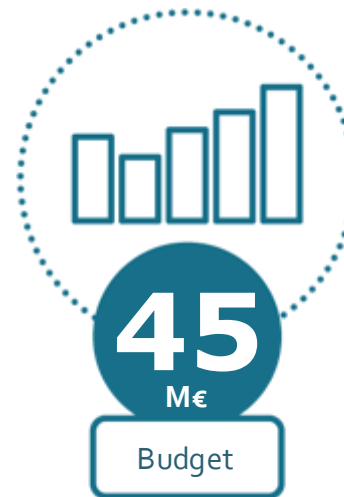
SAFRAN



AIRBUS

- **confiance.ai**: methods and tools for trusted AI.
- High expectations for industry
- **3 groups of scientific challenges** to cover all aspects of trust
 - 1) **Trust and learning data**
 - 2) **Trust and human interaction**
 - 3) **Trust and AI-based system engineering**
- Organization in **7 projects**:
 - EC1: Integration & **use cases**
 - EC2: Process, **methodology** and guidelines
 - EC3: Characterization & **qualification** of trustworthy AI
 - EC4: **Design** for Trustworthy AI
 - EC5: Data, information and knowledge **engineering** for trusted AI
 - EC6: **IVV&Q** strategy toward homologation / **certification**
 - EC7: Target **Embedded AI**

- **confiance.ai**: methods and tools for trusted AI → High expectations for industry
- many scientific challenges (as part of the confiance.ai doctoral programme)
 - **Data** coverage and operational **domain design** ODD in Computer Vision (PhD Thesis of Adrien Le Coz)
 - **Robustness** to 'patch' adversarial attacks in Computer Vision (PhD Thesis of Paul La Barbarie)
 - Robust **Reinforcement** learning (PhD Thesis of Lucas Schott)
 - Statistical control of **Fairness/Bias** in Machine Learning (Stat) (PhD Thesis of Gayane Taturyan)
 - Towards hardware **deployment** using BO & Neural Architecture Search) (PhD Thesis of H Ouertatani)
 - **Monitoring** of (deployed) AI algorithms using conformal prediction (PhD Thesis of Abdelmouaiz Tebjou)

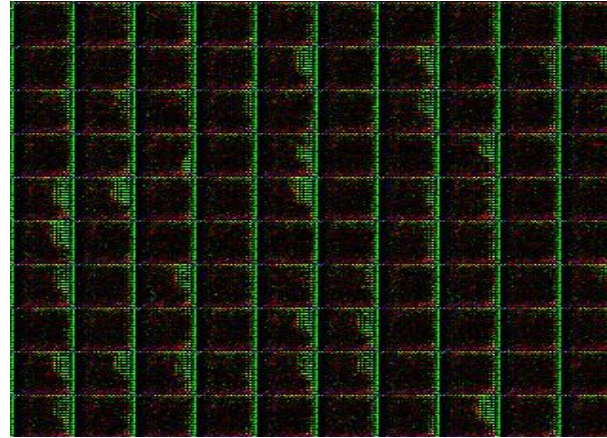


Challenges and industrial applications in

- Hybrid AI: How to exploit industry knowledge of physical (scientific) and symbolic (semantic) nature in data-driven learning models.
- Trustworthy AI: Towards integrating AI into critical system engineering
- **Generative AI for industry:** How to evaluate and advance specialized generative AI models for industrial applications

***GANs** (Goodfellow 2014): A **generator G** and a **discriminator D** subjected to two contradictory training (ie. *adversarial* aspect)

- impressive results in images,...
- **IRT** work advancing the state of the art on the subject: in particular, work on EPI, RTI Con fiance.AI/EC3,4,5 projects.

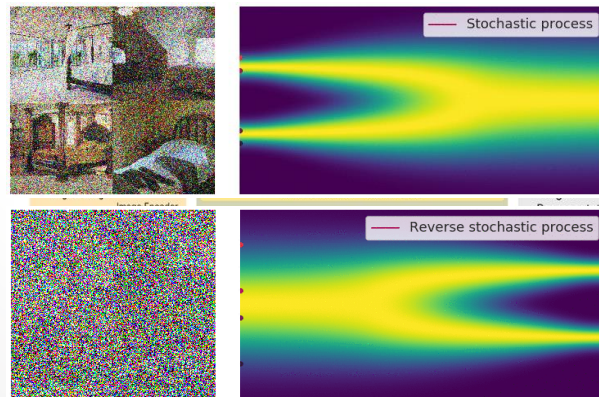


OpenAI

***Diffusion models** (Ho 2020; Yang 2023; Rombach 2022): an unintuitive principle at the basis : progressively **destructure** the input

until it is completely degraded, then **reconstruct** it by reversing the process.

- Excellent performance in image synthesis, despite costly training
- Research work at **IRT** (Con fiance.AI, EC4/Explo; e.g. NeurIPS'23)



Yang Song Blog

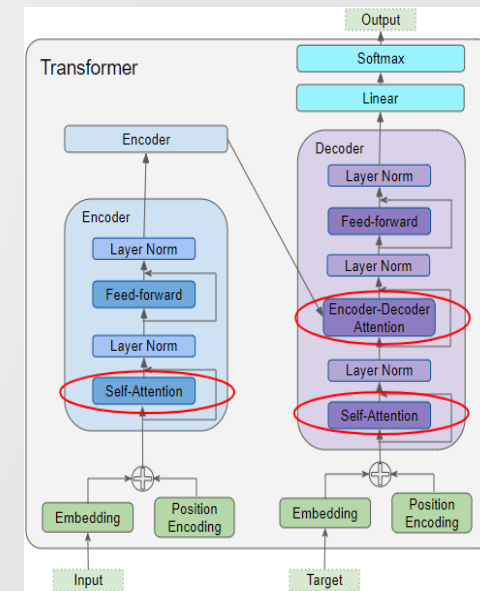
***Transformers** (Vaswani 2017): have revolutionized generative AI, particularly in NLP.

- highly parallelizable (unlike sequential architectures like RNNs)
- Use an AE and relies on an **attention mechanism** to integrate global I/O and context dependencies into a variable-length sequence.

→ High NLP capabilities {eg. ChatGPT-3.5: responses of up to ~ 3000 words}.

→ NLP models and transformers are studied in R&D at IRT

(eg. Con fiance.AI, SMD)



- **Main scientific challenge in GenAI in industry** (Hybridization, Frugality, Multimodalities, Evaluation/Benchmarking, ..)
 - the **frugality** of foundation models (related to data, model, and learning),
 - operating on different **multi-modalities** (beyond text : time-series, diagrams, images..),
 - their **hybridization** to integrate knowledge (expert and or scientific **knowledge**),
 - their **specialization** (eg. fine-tuning, RAG) to different **use cases**,
 - and their **evaluation** to guarantee industrial use,
- Preparation to the implementation of the AI act
- Hybrid AI (GenAI, Physics-Simulation, Data augmentation, Uncertainty Quantification, ..)

- **Hybrid AI**, with its inclusive approach to human knowledge, overcomes the limitations of “classic” AI (based exclusively on data) : The
 - **accuracy** of physical simulations can be improved by hybrid modeling that takes advantage of data.
 - joint use of data and scientific laws **reduces the complexity and cost** of physical simulations.
 - joint use of data & knowledge graphs enables **business expertise to be integrated** and results to be **explained**.

- Approaches that hybridize data and knowledge models (physical/semantic) have emerged fairly recently, and **have not yet reached maturity** ==> R&D efforts are needed to bring the subject to maturity in engineering/industry.

- An avenue in AI to the preparation of the implementation of the AI act for the enterprise, is Trusted AI. Need for the Human in the loop

- **Generative AI** is beginning to make slight progress in industry...

General hybrid

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THANK YOU FOR YOUR ATTENTION

